

Reliable quantum certification for photonic quantum technologies

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[arXiv:1407.4817]

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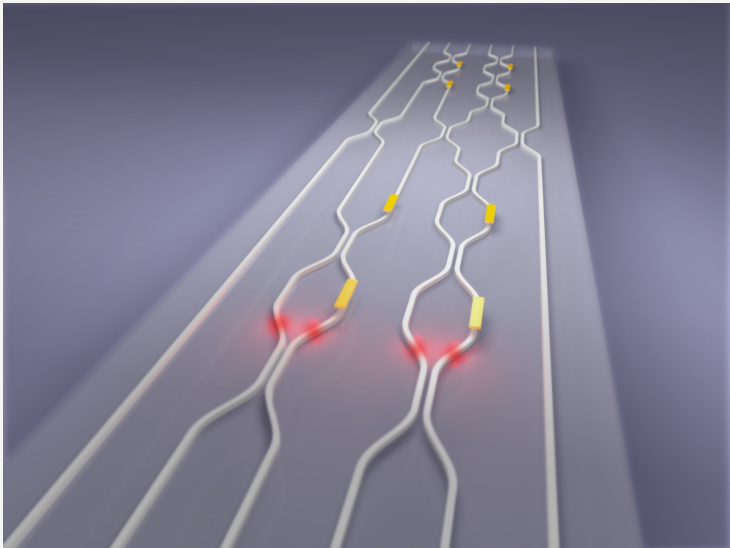
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DPG Spring Meeting 2015, Heidelberg

Photonic quantum technologies



source <http://phys.org/>

Example: BosonSampling

Science

339, 798 (2013):

Boson Sampling on a Photonic Chip

Justin B. Spring,^{1,*} Benjamin J. Metcalfe,¹ Peter C. Humphreys,¹ W. Steven Kolthammer,¹ Xian-Min Jin,^{1,2} Marco Barbieri,¹ Animesh Datta,¹ Nicholas Thomas-Peter,¹ Nathan K. Langford,^{1,3} Dmytro Kundys,⁴ James C. Gates,⁴ Brian J. Smith,¹ Peter G. R. Smith,⁴ Ian A. Walmsley^{1,*}

Quantum computers ideally solve problems such as factoring integers

nature
photonics

LETTERS

PUBLISHED ONLINE: 26 MAY 2013 | DOI: 10.1038/NPHOTON.2013.112

Integrated multimode interferometers with arbitrary designs for photonic boson sampling

Andrea Crespi^{1,3}, Roberto Osellame^{1,2,*}, Roberta Ramponi^{1,3}, Daniel J. Brod³, Ernesto F. Galvão^{1,*}, Nicolò Spagnolo¹, Chiara Vitelli^{1,5}, Enrico Malorino¹, Paolo Mataloni¹ and Fabio Sciarino^{1,4}

The evolution of bosons underlines a fundamental property of quantum mechanics

Efficient experimental validation of photonic boson sampling against the uniform distribution

Nicolò Spagnolo,¹ Chiara Vitelli,^{1,2} Marco Bentivegna,¹ Daniel J. Brod,³ Andrea Crespi,^{4,5} Fulvio Flamini,¹ Sandro Giacomini,¹ Giorgio Milani,¹ Roberta Ramponi,^{4,5} Paolo Mataloni,^{1,6} Roberto Osellame,^{4,5,*} Ernesto F. Galvão,^{3,1} and Fabio Sciarino^{1,6,4}

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Piazza Leonardo da Vinci

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⁶Istituto Nazionale di Ottica (INO)

A boson sampling device is a specialised quantum computer that solves a problem which is strongly believed to be computationally intractable for classical computers [1]. Recently a number of small-scale implementations have been reported [2–5], all based on multi-photon interference.

LETTERS

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nature
photonics

Experimental boson sampling

Max Tillmann^{1,2,*}, Borivoje Dakić, René Heilmann¹, Stefan Nolte³, Alexander Szameit³ and Philip Walther^{1,2,*}

Quantum computers ideally solve problems such as factoring integers

Science

339, 794 (2013):

Photonic Boson Sampling in a Tunable Circuit

Matthew A. Broome,^{1,2,*} Alessandro Fedrizzi,^{1,2} Saleh Rahimi-Keshari,² Justin Dove,³ Scott Aaronson,³ Timothy C. Ralph,² Andrew G. White^{1,2}

nature
photonics

ARTICLES

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On the experimental verification of quantum complexity in linear optics

J. Shadbolt¹, Nicholas J. Russell¹, Nur Ismail¹, Philip Walther¹, Jeremy L. O'Brien¹

BosonSampling with Controllable Distinguishability

Max Tillmann¹, Si-Hui Tan², Sarah E. Stoecckl¹, Barty C. Sanders³, Hubert de Guise⁴, René Heilmann⁵, Stefan Nolte⁶, Alexander Szameit⁶, Philip Walther¹

¹Faculty of Physics, University of Vienna, Boltzmanngasse 5, A-1090 Vienna, Austria

²Singapore University of Technology and Design, 20 Dover Drive, 136882 Singapore

³Institute for Quantum Science and Technology, University of Calgary, Alberta, Canada T2N 1N4

⁴Department of Physics, Lakehead University, Thunder Bay, Ontario, P7B 5E1, Canada and

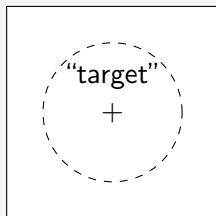
⁵Institute of Applied Physics, Abbe Center of Photonics, 07743 Jena, Germany

Quantum computers are believed to be more powerful than classical computers. The first of these is the fact that quantum computers can solve certain problems more efficiently than classical computers. The second is that quantum computers can solve certain problems more reliably than classical computers. The third is that quantum computers can solve certain problems more accurately than classical computers. The fourth is that quantum computers can solve certain problems more quickly than classical computers. The fifth is that quantum computers can solve certain problems more cheaply than classical computers. The sixth is that quantum computers can solve certain problems more easily than classical computers. The seventh is that quantum computers can solve certain problems more simply than classical computers. The eighth is that quantum computers can solve certain problems more gracefully than classical computers. The ninth is that quantum computers can solve certain problems more elegantly than classical computers. The tenth is that quantum computers can solve certain problems more beautifully than classical computers. The eleventh is that quantum computers can solve certain problems more harmoniously than classical computers. The twelfth is that quantum computers can solve certain problems more pleasantly than classical computers. The thirteenth is that quantum computers can solve certain problems more agreeably than classical computers. The fourteenth is that quantum computers can solve certain problems more suitably than classical computers. The fifteenth is that quantum computers can solve certain problems more conveniently than classical computers. The sixteenth is that quantum computers can solve certain problems more expeditiously than classical computers. The seventeenth is that quantum computers can solve certain problems more speedily than classical computers. 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The twenty-sixth is that quantum computers can solve certain problems more mutually than classical computers. The twenty-seventh is that quantum computers can solve certain problems more collectively than classical computers. The twenty-eighth is that quantum computers can solve certain problems more communally than classical computers. The twenty-ninth is that quantum computers can solve certain problems more societally than classical computers. The thirtieth is that quantum computers can solve certain problems more associatively than classical computers. The thirty-first is that quantum computers can solve certain problems more relationally than classical computers. The thirty-second is that quantum computers can solve certain problems more interrelationally than classical computers. The thirty-third is that quantum computers can solve certain problems more interdependently than classical computers. 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The problem of certification

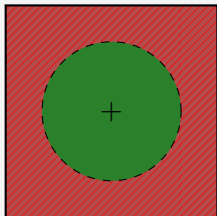
How do you know the device works?

What is certification?



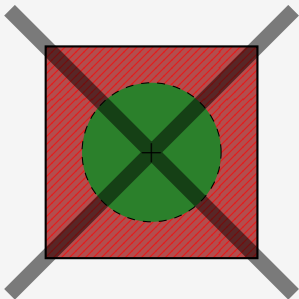
What is certification?

naive



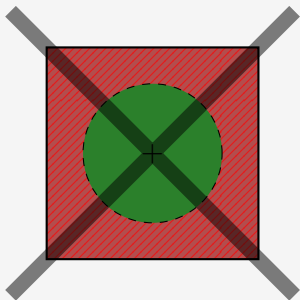
What is certification?

impossible

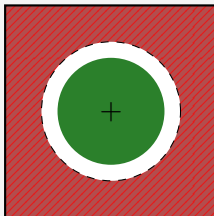


What is certification?

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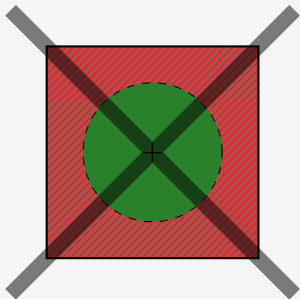


robust

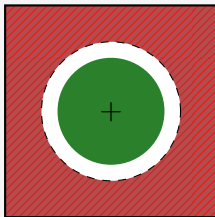


What is certification?

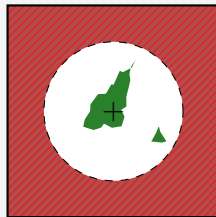
impossible



robust



good enough



Certification as a game

Prover

claims has quantum device

Verifier

only limited measurements

Certification as a game

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Verifier

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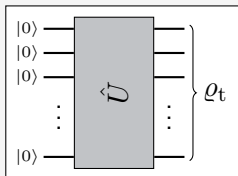
request target state ϱ_t

Certification as a game

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claims to do:



Verifier

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Certification as a game

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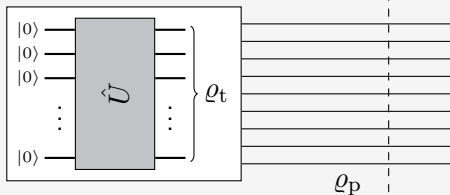
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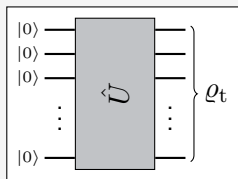


Certification as a game

Prover

claims has quantum device

claims to do:

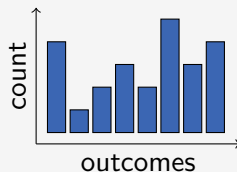


ϱ_p

Verifier

only limited measurements

request target state ϱ_t

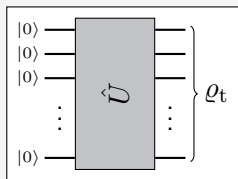


Certification as a game

Prover

claims has **quantum device**

claims to do:

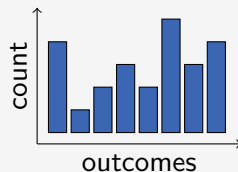


ρ_p

Verifier

only **limited** measurements

request target state ρ_t

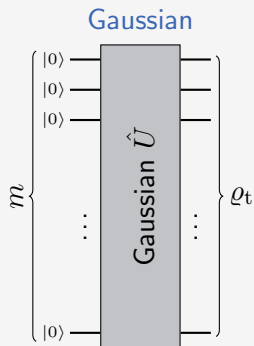


Is $\rho_p \approx \rho_t$?

Number of preparations?

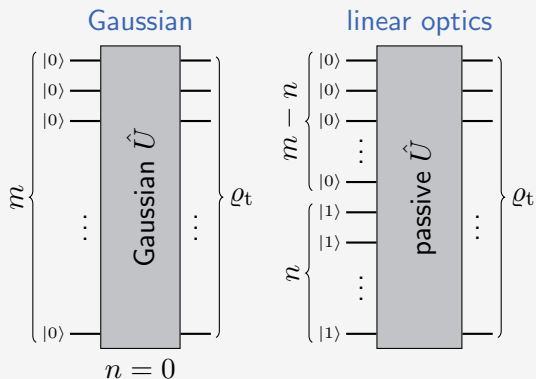
The settings

Three classes of target states:



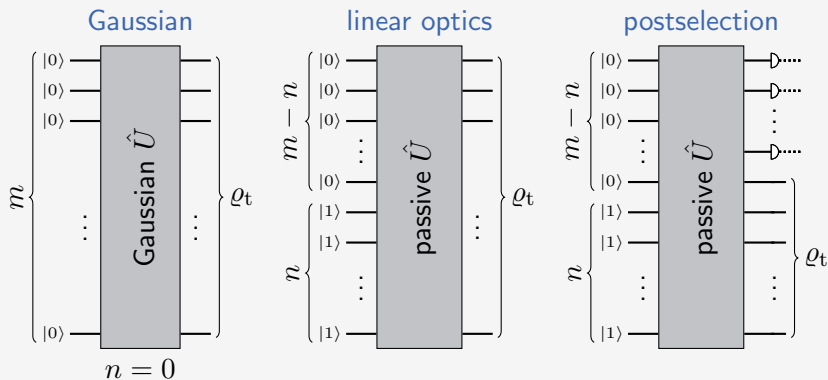
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The settings

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Results

Certification test for n initial photons in m modes

- 1 Choose your target state ρ_t , fix a threshold fidelity F_T , failure probability α , and an estimators error $\epsilon \leq (1 - F_T)/2$.

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Gaussian:

Achieve robust certification for $N \in O\left(\frac{\text{poly}(m)}{\epsilon^2 \log(\frac{1}{1-\alpha})}\right)$.

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linear optics:

Achieve robust certification for $N \in O\left(\frac{m^4(\text{poly}(m)n)^n}{\epsilon^2 \log(\frac{1}{1-\alpha})}\right)$.

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- 4 Estimate fidelity and if $F^* < F_T + \epsilon$ reject, otherwise accept.

postselection:

Achieve certification for
$$N \in O\left(\frac{m^4(\text{poly}(m)n)^n}{P^2 \epsilon^2 \log(\frac{1}{1-\alpha})}\right).$$

Conclusions

- In the Gaussian setting efficient ($\text{poly}(m)$ effort) and robust.

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- In the **linear optics** setting still **robust** and **efficient** in m but not in n .
- For **explicit bounds** (number of preparations, size of acceptance region, ...) and all the fine print (definition of robust certification, post selection, ...) see [\[arXiv:1407.4817\]](#).

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Thank you for your attention!